



Dofinansowane przez Unię Europejską



### **COURSE SPECIFICATION**

| Course code                | full-time programme:           | M#2-S2-ME-PT-115 |  |  |  |  |  |
|----------------------------|--------------------------------|------------------|--|--|--|--|--|
|                            | part-time programme:           |                  |  |  |  |  |  |
| Course title in Polish     | Dynamika układów mechanicznych |                  |  |  |  |  |  |
| Course title in English    | Dynamics of Mechanical Systems |                  |  |  |  |  |  |
| Valid from (academic year) | 2024/2025                      |                  |  |  |  |  |  |

### **GENERAL INFORMATION**

| Programme of study     | MECHANICAL ENGINEERING  |
|------------------------|---|
| Level of qualification | second-cycle  |
| Type of education      | academic  |
| Mode of study          | full-time programme   |
| Specialism             | Design and Manufacturing  |
| Department responsible | Department of Automotive Engineering and Transport  |
| Course leader          | dr inż. Andrzej Zuska   |
| Approved by            | dr hab. Jakub Takosoglu, prof. PŚk, Dean of the Faculty of<br>Mechatronics and Mechanical Engineering |

### **COURSE OVERVIEW**

| Course type                   |                     | specialism-related |  |  |  |  |
|-------------------------------|---------------------|--------------------|--|--|--|--|
| Course status                 |                     | compulsory         |  |  |  |  |
| Language of instruction       |                     | English            |  |  |  |  |
| full-time programme           |                     | Semester I         |  |  |  |  |
| Semester of delivery          | part-time programme | Semester I         |  |  |  |  |
| Pre-requisites                |                     |                    |  |  |  |  |
| Examination required (YES/NO) |                     | NO                 |  |  |  |  |
| ECTS value                    |                     | 2                  |  |  |  |  |

| Mode of instruction |                        | lecture | class | laboratory | project | seminar |
|---------------------|------------------------|---------|-------|------------|---------|---------|
| No. of hours        | full-time<br>programme | 15      |       | 15         |         |         |
| per semester        | part-time<br>programme |         |       |            |         |         |

# LEARNING OUTCOMES

|  | Category of<br>outcome | Outcome<br>code | Course learning outcomes | Corresponding<br>programme<br>outcome code |
|--|------------------------|-----------------|--------------------------|--|
|--|------------------------|-----------------|--------------------------|--|









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| r              | 1  |  |                        |  |  |
|----------------|--|--|------------------------|--|--|
|                | W01  | Has a structured knowledge of the basic concepts<br>and problems of the dynamics of mechanical<br>discrete systems.  | MiBM2_W01<br>MiBM2_W07 |  |  |
|                | W02  | Has a structured knowledge of the modeling of mechanical discrete systems as an oscillating system.  | MiBM2_W01<br>MiBM2_W07 |  |  |
| Knowledge      | W03  | Has a structured knowledge of the components of the models, with particular emphasis on the susceptible components.  | MiBM2_W01<br>MiBM2_W07 |  |  |
|                | W04 W04 Has a basic theoretical knowledge of the construction of the equations of vibration of discrete systems. Is familiar with Lagrange's Equations of the second kind. |  |                        |  |  |
|                | W05  | Has basic theoretical knowledge of selected issues<br>of classical analysis of mechanical vibrations of<br>discrete systems (time domain analysis).                                      | MiBM2_W01<br>MiBM2_W07 |  |  |
|                | W06  | Has basic theoretical knowledge of spectral analysis of vibrations.  | MiBM2_W01<br>MiBM2_W07 |  |  |
|                | U01  | Can determine the characteristics of susceptible<br>elements (linear and nonlinear), used in modeling<br>the dynamics of discrete systems.   | MiBM2_U02<br>MiBM2_U11 |  |  |
|                | U02  | Can apply the operator method to determine the characteristics of linear susceptible elements.   | MiBM2_U02<br>MiBM2_U11 |  |  |
| Skills         | U03  | Be able to build an algorithm and computational<br>program for vibration analysis of a mechanical<br>model of a discrete system in the time domain (in<br>different coordinate systems). | MiBM2_U02<br>MiBM2_U11 |  |  |
|                | U04  | Can build an algorithm and computational program<br>to analyze the vibration of a mechanical model of a<br>discrete system in the frequency domain.                                      | MiBM2_U02<br>MiBM2_U11 |  |  |
| Competence K01 |  | Understands the need for and knows the possibilities of improving his professional skills.   | MiBM2_K01              |  |  |

# COURSE CONTENT

| Mode of     |                |
|-------------|----------------|
| instruction | Topics covered |







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|            | Basic concepts and problems of vertical dynamics of mechanical discrete systems.   |  |  |  |  |  |  |  |
|------------|--|--|--|--|--|--|--|--|
|            | Features of fundamental motion and perturbations of fundamental motion.  |  |  |  |  |  |  |  |
|            | Assumptions made in classical vibration theory of discrete systems. Modeling in  |  |  |  |  |  |  |  |
|            | machine dynamics.  |  |  |  |  |  |  |  |
|            | The process of building dynamic models: determination of the structure of the  |  |  |  |  |  |  |  |
|            | model, description of mass quantities, coordinates of the system, determination of the   |  |  |  |  |  |  |  |
|            | number of degrees of freedom, determination of data and description of the forcing   |  |  |  |  |  |  |  |
|            | acting on the system.  |  |  |  |  |  |  |  |
|            | Components of a dynamic model. Mass elements: methods of experimental  |  |  |  |  |  |  |  |
|            | determination and approximate estimation of moments of inertia of the entire discrete  |  |  |  |  |  |  |  |
|            | system and other model bodies. Deformable elements - basic models of linear  |  |  |  |  |  |  |  |
|            | elements. Operator method of determining characteristics of linear elements; operator  |  |  |  |  |  |  |  |
|            | stiffness. Characteristics of parallel and series connection of two linear elements.   |  |  |  |  |  |  |  |
|            | Nonlinear prone elements. Methods of determining the characteristics of nonlinear  |  |  |  |  |  |  |  |
|            | elements. Method of extracting the characteristics: elastic and damping characteristics  |  |  |  |  |  |  |  |
|            | from the characteristics determined in the form of an inelastic hysteresis loop. The   |  |  |  |  |  |  |  |
|            | concept of a weakly nonlinear element - linearization of nonlinear characteristics of susceptible elements. Vibration excitations - classification of signals.           |  |  |  |  |  |  |  |
|            | Construction of the equations of vibration of a mechanical discrete system.  |  |  |  |  |  |  |  |
|            | Lagrange equations of the second kind. Total kinetic and potential energy of the   |  |  |  |  |  |  |  |
| lecture    | system. Use of Lagrange's equations to derive the equations of motion of a spatial   |  |  |  |  |  |  |  |
|            | model of a discrete system with 3 degrees of freedom. Use of the operator method to  |  |  |  |  |  |  |  |
|            | introduce linear susceptible elements with different characteristics into the model.   |  |  |  |  |  |  |  |
|            | Introduction of the postulate of symmetry of the model with respect to the xOz-plane -   |  |  |  |  |  |  |  |
|            | decoupling of vibrations in the longitudinal and transverse planes. Notation of  |  |  |  |  |  |  |  |
|            | equations of vibration in matrix form.   |  |  |  |  |  |  |  |
|            | Selected issues of classical analysis of vibrations of a mechanical discrete system  |  |  |  |  |  |  |  |
|            | (analysis in the time domain) Natural frequencies of systems with multiple degrees of  |  |  |  |  |  |  |  |
|            | freedom - the method of determination. The problem of decoupling of vibrations of  |  |  |  |  |  |  |  |
|            | partial sub-systems (Mandelstam's conditions).   |  |  |  |  |  |  |  |
|            | Spectral analysis of vibrations of a mechanical discrete system. Spectral analysis   |  |  |  |  |  |  |  |
|            | of periodic oscillations. Fourier series. Discrete (strip) spectra: amplitude-frequency  |  |  |  |  |  |  |  |
|            | and phase-frequency. Fourier integral transformation. Properties of the Fourier transform. Spectra of non-periodic oscillations (continuous spectra). Application of the |  |  |  |  |  |  |  |
|            | Fourier transform to solve the equation of vibration of a system with one degree of  |  |  |  |  |  |  |  |
|            | freedom. Spectral transmittance of a system. Graphical representation of   |  |  |  |  |  |  |  |
|            | transmittance: real and imaginary part of transmittance; amplitude-frequency and   |  |  |  |  |  |  |  |
|            | phase-frequency characteristics (modulus and argument). Transmittance of the input   |  |  |  |  |  |  |  |
|            | of a system with kinematic forcing. Spectral analysis of vibrations of systems with  |  |  |  |  |  |  |  |
|            | multiple degrees of freedom. Transmittance matrix and its properties.  |  |  |  |  |  |  |  |
|            | Determination of characteristics of susceptible elements used in modeling a) linear  |  |  |  |  |  |  |  |
|            | elements b) elements with nonlinear and complex characteristics.   |  |  |  |  |  |  |  |
|            | Application of the operator method to determine the characteristics of linear prone  |  |  |  |  |  |  |  |
|            | elements. Determination of characteristics of parallel and series connection of two  |  |  |  |  |  |  |  |
| laboratory | susceptible elements.  |  |  |  |  |  |  |  |
|            | Development of a program to analyze the motion of the model in solid coordinates.  |  |  |  |  |  |  |  |
|            | Develop a program to analyze the motion of the model in point coordinates.   |  |  |  |  |  |  |  |
|            | Development of a program to determine the natural frequency of the system.   |  |  |  |  |  |  |  |
|            | Development of a program to determine the transmittance modulus and power spectral   |  |  |  |  |  |  |  |
|            | densities of the system response.  |  |  |  |  |  |  |  |

# ASSESSMENT METHODS

| Outcome | Methods of assessmentOralWritten<br>examinationTestProjectReportOther |  |   |  |  |  |  |  |  |
|---------|---|--|---|--|--|--|--|--|--|
| code    |   |  |   |  |  |  |  |  |  |
| W01     |   |  | Х |  |  |  |  |  |  |
| W02     |   |  | Х |  |  |  |  |  |  |





Fundusze Europejskie dla Rozwoju Społecznego



Rzeczpospolita Polska Dofinansowane przez Unię Europejską



| W03 |  | Х |   |   |
|-----|--|---|---|---|
| W04 |  | Х |   |   |
| W05 |  | Х |   |   |
| W06 |  | Х |   |   |
| U01 |  |   | Х |   |
| U02 |  |   | Х |   |
| U03 |  |   | Х |   |
| U04 |  |   | Х |   |
| K01 |  |   |   | Х |

#### ASSESSMENT TYPE AND CRITERIA

| Mode of<br>instruction | Assessment type               | Assessment criteria   |
|------------------------|-------------------------------|---|
| lecture                | non-examination<br>assessment | Successful completion of the colloquium, obtaining at least 50% of the points |
| laboratory             | non-examination<br>assessment | Passing the reports, obtaining at least 50% of the points.                    |

#### OVERALL STUDENT WORKLOAD

|     | ECTS weighting   |                  |            |        |   |   |     |      |        |      |      |      |
|-----|--|------------------|------------|--------|---|---|-----|------|--------|------|------|------|
|     |  | Student workload |            |        |   |   |     |      |        | Unit |      |      |
| No. | Activity type  |                  | -          | ll-tin | - |   |     | •    | rt-tir |      |      |      |
|     |  | L                | L C Lb P S |        |   | L | C C | gran | P      | S    |      |      |
| 1.  | Scheduled contact hours  |                  | C          |        | Γ | 3 |     | C    |        | Г    | 3    | h    |
|     |  | 15               |            | 15     |   |   |     |      |        |      |      |      |
| 2.  | Other contact hours (office hours, examination)                          | 2                | 2 2        |        |   |   |     |      |        |      | h    |      |
| 3.  | Total number of contact hours  |                  | 34         |        |   |   |     |      |        | h    |      |      |
| 4.  | Number of ECTS credits for contact<br>hours                              |                  | 1,4        |        |   |   |     |      |        |      | ECTS |      |
| 5.  | Number of independent study hours  |                  | 16         |        |   |   |     |      |        |      | h    |      |
| 6.  | Number of ECTS credits for<br>independent study hours                    |                  | 0,6        |        |   |   |     |      |        |      | ECTS |      |
| 7.  | Number of practical hours  |                  | 25         |        |   |   |     |      |        | h    |      |      |
| 8.  | Number of ECTS credits for<br>practical hours                            | 1,0              |            |        |   |   |     |      | ECTS   |      |      |      |
| 9.  | Total study time   | 50               |            |        |   | h |     |      |        |      |      |      |
| 10. | ECTS credits for the course<br>1 ECTS credit = 25-30 hours of study time |                  |            |        |   |   | 2   |      |        |      |      | ECTS |

#### READING LIST

- 1. Mitschke M. Dynamika samochodu. Drgania. WKiŁ, Warszawa, 1989.
- 2. Kasprzyk T., Prochowski L. Obciążenia dynamiczne zawieszeń. WKiŁ, Warszawa, 1990.
- Osiecki J., Gromadowski T., Stępiński B., Badania Pojazdów Samochodowych i ich zespołów na symulacyjnych stanowiskach badawczych. Wydawnictwo Instytutu Technologii i Eksploatacji, Radom, 2006.









Rzeczpospolita Polska





 Kamiński E., Pokorski J. Dynamika zawieszeń i układów napędowych pojazdów samochodowych. WKiŁ, Warszawa, 1983. 5. Blajer W. Metody dynamiki układów wieloczłonowych. Wyd. Politechniki Radomskiej, Radom, 1998.

