

## MODULE DESCRIPTION

|                          |                        |
|--------------------------|------------------------|
| Module code              | <b>Z-0085z</b>         |
| Module name              | <b>Algebra Liniowa</b> |
| Module name in English   | <b>Linear Algebra</b>  |
| Valid from academic year | <b>2016/2017</b>       |

## A. MODULE PLACEMENT IN THE SYLLABUS

|                                       |   |
|---------------------------------------|---|
| Field of study                        | <b>Management and Production Engineering</b>                              |
| Level of education                    | <b>1st degree</b><br><i>(1st degree / 2nd degree)</i>                     |
| Studies profile                       | <b>General</b><br><i>(general / practical)</i>                            |
| Form and method of conducting classes | <b>Full-time</b><br><i>(full-time / part-time)</i>                        |
| Specialisation                        | <b>All</b>  |
| Unit conducting the module            | <b>The Department of Applied Computer Science and Applied Mathematics</b> |
| Module co-ordinator                   | <b>Beata Maciejewska, PhD</b>   |
| Approved by:                          |   |

## B. MODULE OVERVIEW

|   |  |
|---|--|
| Type of subject/group of subjects           | <b>Basic</b><br><i>(basic / major / specialist subject / conjoint / other HES)</i> |
| Module status                               | <b>Compulsory</b><br><i>(compulsory / non-compulsory)</i>                          |
| Language of conducting classes              | <b>English</b>   |
| Module placement in the syllabus - semester | <b>1st semester</b>  |
| Subject realisation in the academic year    | <b>Winter semester</b><br><i>(winter semester/ summer)</i>                         |
| Initial requirements                        | <b>No requirements</b><br><i>(module codes / module names)</i>                     |
| Examination                                 | <b>No</b><br><i>(yes / no)</i>   |
| Number of ECTS credit points                | <b>3</b>   |

| Method of conducting classes | Lecture   | Classes   | Laboratory | Project | Other |
|------------------------------|-----------|-----------|------------|---------|-------|
| Per semester                 | <b>15</b> | <b>15</b> |            |         |       |

### C. TEACHING RESULTS AND THE METHODS OF ASSESSING TEACHING RESULTS

|                      |  |
|----------------------|--|
| <b>Module target</b> | The aim of the module is to familiarise students with the matrix analysis, the methods of solving systems of linear equations, the complex numbers field, with calculus of vectors and analytic geometry in the three-dimensional space. |
|----------------------|--|

| Effect symbol | Teaching results   | Teaching methods<br>(l/c/lab/p/other) | Reference to subject effects | Reference to effects of a field of study |
|---------------|--|---------------------------------------|------------------------------|--|
| W_01          | A student has basic knowledge of complex numbers, matrix analysis and calculus of vectors, the methods of solving linear equations and analytic geometry.  | l/c                                   | K_W01                        | T1A_W01<br>T1A_W07                       |
| U_01          | A student can apply matrix calculus to solve matrix equations and to solve systems of linear equations.  | l/c                                   | K_U01                        | TA1_U01                                  |
| U_02          | A student can evaluate the usefulness of familiar methods concerning solving equations and systems of linear equations; a student is also able to select the appropriate method in order to solve a system of equations. | l/c                                   | K_U02                        | TA1_U02                                  |
| U_03          | A student is able to geometrically interpret the basic concepts of complex numbers, knows how to perform calculations in the set of complex numbers, and solve equations in the complex domain.                          | l/c                                   | K_U01                        | TA1_U01                                  |
| U_04          | Student is able to geometrically interpret solutions of linear equations systems. He can connect the basic concepts of analytical geometry with vector calculus.   | l/c                                   | K_U01<br>K_U02               | TA1_U01<br>TA1_U02                       |
| K_01          | A student understands the need to improve the acquired skills and knowledge. A student can comprehend the elementary relationship between the workload and its effect.   | c                                     | K_K01                        | TA1_K01                                  |
| K_02          | A student knows the possibilities of improving the acquired knowledge and skills as regards linear algebra and analytic geometry.  | l/c                                   | K_K01                        | TA1_K01                                  |
| K_03          | A student is aware of the responsibility for his/her own work and is ready to comply with the rules of team work and to bear the consequences of the tasks completed collectively.                                       | c                                     | K_K04                        | T1A_K03<br>T1A_K04                       |

#### Teaching contents:

##### 1. Teaching contents as regards lectures

| Lecture number | Teaching contents  | Reference to teaching results for a module |
|----------------|--|--|
| 1              | Matrices: types of matrices, operations and calculations on matrices and their properties.   | W_01<br>K_01<br>K_02                       |
| 2              | Determinant of a quadratic matrix: the notion of a matrix determinant and basic properties. Laplace's rule. Inverse matrix. Solving matrix equations.      | W_01<br>K_01<br>K_02                       |
| 3              | Systems of linear equations. Cramer's rule. Matrix method of solving Cramer's systems. Solving systems of equations with the elementary operations method. | W_01<br>K_01<br>K_02                       |
| 4              | Vectors in space. Operations on vectors. Dot product of vectors. Cross product of vectors.   | W_01<br>K_01<br>K_02                       |

|   |  |                                      |
|---|--|--------------------------------------|
| 5 | Analytic geometry in the three-dimensional space: a straight line and plane in space.  | W_01<br>K_01<br>K_02                 |
| 6 | Relative position of points, straight lines and planes.  | W_01<br>K_01<br>K_02                 |
| 7 | Complex numbers. Rectangular form of a complex number and calculations on the set of complex numbers. Polar form of a complex number – geometric interpretation. Euler's formula. De Moivre's formula. A root of complex number. Solving polynomial equations in a complex domain. | W_01<br>K_01<br>K_02                 |
| 8 | A test.  | W_01<br>U_01<br>U_02<br>U_03<br>U_04 |

## 2. Teaching contents as regards classes

| Class number | Teaching contents   | Reference to teaching results for a module   |
|--------------|---|--|
| 1            | Matrices: operations on matrices and the properties of operations. Matrix determinant – the definition and basic properties.  | W_01<br>U_01<br>K_01<br>K_02<br>K_03         |
| 2            | Inverse matrix and its application in solving matrix equations.   | W_01<br>U_01<br>K_01<br>K_02<br>K_03         |
| 3            | Systems linear equations. The application of determinants in solving systems of linear equations (Cramer's rule). Matrix method of solving Cramer's systems.  | W_01<br>U_01<br>U_02<br>K_01<br>K_02<br>K_03 |
| 4            | Solving systems of equations with the elementary operations method.   | W_01<br>U_01<br>U_02<br>K_01<br>K_02<br>K_03 |
| 5            | Operations on vectors in space. Dot and cross products of vectors.  | W_01<br>U_04<br>K_01<br>K_02<br>K_03         |
| 6            | The description of a straight line and a plane in space. Relative position of points, straight line and a plane in space.   | W_01<br>U_04<br>K_01<br>K_02<br>K_03         |
| 7            | Complex numbers in an rectangular form and basic operations on complex numbers. Geometric interpretation of a complex number. A root of complex number. Solving polynomial equations in a complex domain. | W_01<br>U_03<br>K_01<br>K_02<br>K_03         |
| 8            | A test.   | W_01<br>U_01<br>U_02                         |

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|--|--|--------------|
|  |  | U_03<br>U_04 |
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### 3. Teaching contents as regards laboratory classes

| Laboratory class number | Teaching contents | Reference to teaching results for a module |
|-------------------------|-------------------|--|
|                         |                   |  |
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|                         |                   |  |

### 4. The characteristics of project assignments

## The methods of assessing teaching results

| Effect symbol | Methods of assessing teaching results<br><i>(assessment method, including skills – reference to a particular project, laboratory assignments, etc.)</i> |
|---------------|---|
| W_01          | Tests, a student's initiative during the classes, and homework assignments.   |
| U_01          | Tests, a student's initiative during the classes, and homework assignments.   |
| U_02          | Tests, a student's initiative during the classes, and homework assignments.   |
| U_03          | Tests, a student's initiative during the classes, and homework assignments.   |
| U_04          | Tests, a student's initiative during the classes, and homework assignments.   |
| K_01          | Observing a student's involvement during his/her independent work during the classes; a discussion during the lectures and classes.                     |
| K_02          | Observing a student's involvement during his/her independent work during the classes; a discussion during the lectures and classes.                     |
| K_03          | Observing a student's involvement during his/her independent work during the classes; a discussion during the lectures and classes.                     |

## D. STUDENT'S INPUT

| ECTS credit points |   |                           |
|--------------------|---|---------------------------|
|                    | Type of student's activity  | Student's workload        |
| 1                  | Participation in lectures   | 15                        |
| 2                  | Participation in classes  | 15                        |
| 3                  | Participation in laboratories   |                           |
| 4                  | Participation in tutorials (2-3 times per semester)   | 10                        |
| 5                  | Participation in project classes  |                           |
| 6                  | Project tutorials   |                           |
| 7                  | Participation in an examination   |                           |
| 8                  |   |                           |
| 9                  | <b>Number of hours requiring a lecturer's assistance</b>  | <b>40</b><br><i>(sum)</i> |
| 10                 | <b>Number of ECTS credit points which are allocated for assisted work</b><br><i>(1 ECTS point=25-30 hours)</i>          | <b>1.5</b>                |
| 11                 | Unassisted study of lecture subjects  | 10                        |
| 12                 | Unassisted preparation for classes  | 16                        |
| 13                 | Unassisted preparation for tests  | 10                        |
| 14                 | Unassisted preparation for laboratories   |                           |
| 15                 | Preparing reports   |                           |
| 15                 | Preparing for a final laboratory test   |                           |
| 17                 | Preparing a project or documentation  |                           |
| 18                 | Preparing for an examination  | 4                         |
| 19                 |   |                           |
| 20                 | <b>Number of hours of a student's unassisted work</b>   | <b>40</b><br><i>(sum)</i> |
| 21                 | <b>Number of ECTS credit points which a student receives for unassisted work</b><br><i>(1 ECTS point=25-30 hours)</i>   | <b>1.5</b>                |
| 22                 | <b>Total number of hours of a student's work</b>  | <b>80</b>                 |
| 23                 | <b>ECTS points per module</b><br><i>1 ECTS point=25-30 hours</i>  | <b>3</b>                  |
| 24                 | <b>Work input connected with practical classes</b><br><i>Total number of hours connected with practical classes</i>     | <b>41</b>                 |
| 25                 | <b>Number of ECTS credit points which a student receives for practical classes</b><br><i>(1 ECTS point=25-30 hours)</i> | <b>1.5</b>                |

## E. LITERATURE

|                 |   |
|-----------------|---|
| Literature list | <ol style="list-style-type: none"> <li>Gdowski B., Pluciński E., <i>Zadania z rachunku wektorowego i geometrii analitycznej</i>, PWN, Warszawa 1982.</li> <li>Grysa K., <i>Zastosowania matematyki w zarządzaniu i ekonomii. Część I. Elementy algebry</i>, Wydawnictwo Politechniki Świętokrzyskiej, Kielce 2003.</li> <li>Hożejowska S., Hożejowski L., Maciąg A., <i>Matematyka w zadaniach dla studiów ekonomiczno-technicznych</i>, Wydawnictwo Politechniki Świętokrzyskiej, Kielce 2003.</li> <li>Trajdos T., <i>Matematyka. Część III</i>, Wydawnictwa Naukowo-Techniczne, Warszawa 1981.</li> <li>Skrypt z Algebry w formie elektronicznej zamieszczony na stronie: <a href="http://wzimk-moodle.tu.kielce.pl/">http://wzimk-moodle.tu.kielce.pl/</a></li> </ol> |
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| Module website |  |
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