

MODULE SPECIFICATION

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| Module code | |
| Module title in Polish | Matematyka III |
| Module title in English | Mathematics 3 |
| Module running from the academic year | 2016/2017 |

A. MODULE IN THE CONTEXT OF THE PROGRAMME OF STUDY

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| Field of study | Civil Engineering |
| Level of qualification | First cycle <i>(first cycle, second cycle)</i> |
| Studies profile | Academic <i>(academic/practical)</i> |
| Mode of study | Full-time <i>(full-time / part-time)</i> |
| Specialism | |
| Organisational unit responsible for module delivery | The Department of Mathematics |
| Module co-ordinator | Maciej Sękalski, PhD Monika Skóra, PhD |
| Approved by | Marek Iwański, Professor |

B. MODULE OVERVIEW

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| Module type | Core module <i>(core/programme-specific/elective HES*)</i> |
| Module status | Compulsory module <i>(compulsory / non-compulsory)</i> |
| Language of module delivery | English |
| Semester in the programme of study in which the module is taught | Semester 2 |
| Semester in the academic year in which the module is taught | Summer semester <i>(winter / summer)</i> |
| Pre-requisites | None <i>(module code/module title, where appropriate)</i> |
| Examination required | Yes <i>(yes / no)</i> |
| ECTS credits | 6 |

| Mode of instruction | lectures | classes | laboratories | project | others |
|---------------------------------|-----------|-----------|--------------|---------|--------|
| Total hours per semester | 15 | 30 | | | |

* elective HES – elective modules in the Humanities and Economic and Social Sciences

C. LEARNING OUTCOMES AND ASSESSMENT METHODS

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| Module aims | The aim of the module includes acquainting students with basic types of differential equations. Other aims include: indicating the methods of examining functions with two variables; defining a double integral and line integrals and indicating the applications of these applications concerning these tools to calculate surface areas of plane, curved-arches length, side surfaces, and volume of solids. |
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| Module outcome code | Module learning outcomes | Mode of instruction (l/c/lab/p/ others) | Corresponding programme outcome code | Corresponding discipline-specific outcome code |
|---------------------|---|---|--------------------------------------|--|
| W_01 | A student can recognise the types of differential equations. | l/c | B_W01 | T1A_W01 T1A_W07 |
| W_02 | A student can define partial derivatives of functions and (with the use of them) describe the description of a function with two variables (an extreme and a directional derivative). | l/c | B_W01 | T1A_W01 T1A_W07 |
| W_03 | A student is able to characterise the behaviour of an implicit function with one variable. | l/c | B_W01 | T1A_W01 T1A_W07 |
| W_04 | A student is able to select the methods of calculating double and contour integrals; a student can also indicate geometrical and technical application of an integral calculus. | l/c | B_W01 | T1A_W01 T1A_W07 |
| U_01 | A student is capable of making calculations. | c | B_U01 | T1A_U08 T1A_U09 |
| U_02 | A student can solve simple ordinary differential equations. | c | B_U01 | T1A_U08 T1A_U09 |
| U_03 | A student can calculate partial derivative and apply them to examine critical points of functions with two variables as well as examining implicit functions. | c | B_U01 | T1A_U08 T1A_U09 |
| U_04 | A student can calculate double and line integrals; a student can use them in geometry and engineering applications. | c | B_U01 | T1A_U08 T1A_U09 |
| K_01 | A student is aware of the responsibility for his/her own work. | l/c | B_K02 | T1A_K02 T1A_K05 T1A_K07 |
| K_02 | A student understands the necessity of continuous education and raising his/her competences as regards mathematical methods utilised to solve typical engineering problems. | l/c | B_K03 | T1A_K01 T1A_K05 T1A_K06 |

Module content:

1. Topics to be covered in the lectures

| No. | Topics | Module outcome code |
|-----|---|------------------------|
| 1 | Differential equations. Equations with separated variables. First-order linear equations, variation of parameters method. | W_01, K_01, K_02 |
| 2 | Linear differential equations with constant coefficients, the method of predictions. | W_01, K_01, K_02 |
| 3 | Functions with two variables, partial derivatives, and a directional derivative. | W_02, K_01, K_02 |

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| 4 | An implicit function with one variable. Critical points of a function with two variables. | W_02, W_03 K_01, K_02 |
| 5 | A double integral, volume. Calculating double integrals. | W_04, K_01, K_02 |
| 6 | The change of variables in a double integral. Sample applications to calculate plane surface areas and the volume of solids. | W_04, K_01, K_02 |
| 7 | Line undirected integrals. A vector field and definite integral. Physical applications. Green's theorem. | W_04, K_01, K_02 |

2. Topics to be covered in the classes

| No. | Topics | Module outcome code |
|-----|---|---------------------------------|
| 1 | Differential equations. Equations with separated variables. | U_01, U_02, K_01, K_02 |
| 2 | First-order linear equations, variation of parameters method. | U_01, U_02, K_01, K_02 |
| 3 | Linear differential equations with constant variables, the method of predictions. | U_01, U_02, K_01, K_02 |
| 4 | Partial derivatives, a directional derivative, function gradient. | U_01, U_03, K_01, K_02 |
| 5 | An implicit function with one variable. | U_01, U_03, K_01, K_02 |
| 6 | Critical points of a function with two variables. | U_01, U_03, K_01, K_02 |
| 7 | The smallest and greatest value of a function in a closed and limited area. | U_01, U_03, K_01, K_02 |
| 8 | Second-order curves. Second-order surface areas. | U_01, U_04, K_01, K_02 |
| 9 | Calculating a double integral. Fubini's theorem. | U_01, U_04, K_01, K_02 |
| 10 | The change in the order of integration. | U_01, U_04, K_01, |

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|----|--|---------------------------------|
| | | K_02 |
| 11 | The change of variables in a double integral. | U_01, U_04, K_01, K_02 |
| 12 | Calculating the volume of solids as well as surface areas with the use of a double integral. | U_01, U_04, K_01, K_02 |
| 13 | Contour undirected integrals. Calculating curved arches. | U_01, U_04, K_01, K_02 |
| 14 | A definite contour integral. The work of a vector field along a curved line. | U_01, U_04, K_01, K_02 |
| 15 | Green's theorem and its application. | U_01, U_04, K_01, K_02 |

3. Topics to be covered in the laboratories

4. Topics to be covered in the projects

Assessment methods

| Module outcome code | Assessment methods <i>(Method of assessment; for module skills – reference to specific project, laboratory and similar tasks)</i> |
|---------------------|--|
| W_01 | A written test and a written examination |
| W_02 | A written test and a written examination |
| W_03 | A written test and a written examination |
| W_04 | A written test and a written examination |
| U_01 | A written test and a written examination |
| U_02 | A written test and a written examination |
| U_03 | A written test and a written examination |
| U_04 | A written test and a written examination |
| K_01 | Observing a student's involvement during the classes, a discussion during the classes |
| K_02 | Observing a student's involvement during the classes, a discussion during the classes |

C. STUDENT LEARNING ACTIVITIES

| ECTS summary | | |
|--------------|---|------------------------|
| | Type of learning activity | Study time/ credits |
| 1 | Contact hours: participation in lectures | 15 |
| 2 | Contact hours: participation in classes | 30 |
| 3 | Contact hours: participation in laboratories | |
| 4 | Contact hours: attendance at office hours (2-3 appointments per semester) | 8 |
| 5 | Contact hours: participation in project-based classes | |
| 6 | Contact hours: meetings with a project module leader | |

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|----|---|-----------------------------|
| 7 | Contact hours: attendance at an examination | 4 |
| 8 | | |
| 9 | Number of contact hours | 57 <i>(total)</i> |
| 10 | Number of ECTS credits for contact hours <i>(1 ECTS credit =25-30 hours of study time)</i> | 2.3 |
| 11 | Private study hours: background reading for lectures | 15 |
| 12 | Private study hours: preparation for classes | 23 |
| 13 | Private study hours: preparation for tests | 30 |
| 14 | Private study hours: preparation for laboratories | |
| 15 | Private study hours: writing reports | |
| 16 | Private study hours: preparation for a final test in laboratories | |
| 17 | Private study hours: preparation of a project/a design specification | |
| 18 | Private study hours: preparation for an examination | 25 |
| 19 | | |
| 20 | Number of private study hours | 93 <i>(total)</i> |
| 21 | Number of ECTS credits for private study hours <i>(1 ECTS credit =25-30 hours of study time)</i> | 3.7 |
| 22 | Total study time | 150 |
| 23 | Total ECTS credits for the module <i>(1 ECTS credit =25-30 hours of study time)</i> | 6 |
| 24 | Number of practice-based hours <i>Total practice-based hours</i> | 8 |
| 25 | Number of ECTS credits for practice-based hours <i>(1 ECTS credit =25-30 hours of study time)</i> | 0.3 |